

## Chapter Five

# MAGNETISM AND MATTER



### MCQ I

- 5.1** A toroid of  $n$  turns, mean radius  $R$  and cross-sectional radius  $a$  carries current  $I$ . It is placed on a horizontal table taken as  $x$ - $y$  plane. Its magnetic moment  $\mathbf{m}$
- (a) is non-zero and points in the  $z$ -direction by symmetry.
  - (b) points along the axis of the toroid ( $\mathbf{m} = m\hat{\phi}$ ).
  - (c) is zero, otherwise there would be a field falling as  $\frac{1}{r^3}$  at large distances outside the toroid.
  - (d) is pointing radially outwards.
- 5.2** The magnetic field of Earth can be modelled by that of a point dipole placed at the centre of the Earth. The dipole axis makes an angle of  $11.3^\circ$  with the axis of Earth. At Mumbai, declination is nearly zero. Then,
- (a) the declination varies between  $11.3^\circ$  W to  $11.3^\circ$  E.
  - (b) the least declination is  $0^\circ$ .

- (c) the plane defined by dipole axis and Earth axis passes through Greenwich.
- (d) declination averaged over Earth must be always negative.

**5.3** In a permanent magnet at room temperature

- (a) magnetic moment of each molecule is zero.
- (b) the individual molecules have non-zero magnetic moment which are all perfectly aligned.
- (c) domains are partially aligned.
- (d) domains are all perfectly aligned.

**5.4** Consider the two idealized systems: (i) a parallel plate capacitor with large plates and small separation and (ii) a long solenoid of length  $L \gg R$ , radius of cross-section. In (i)  $\mathbf{E}$  is ideally treated as a constant between plates and zero outside. In (ii) magnetic field is constant inside the solenoid and zero outside. These idealised assumptions, however, contradict fundamental laws as below:

- (a) case (i) contradicts Gauss's law for electrostatic fields.
- (b) case (ii) contradicts Gauss's law for magnetic fields.
- (c) case (i) agrees with  $\oint \mathbf{E} \cdot d\mathbf{l} = 0$ .
- (d) case (ii) contradicts  $\oint \mathbf{H} \cdot d\mathbf{l} = I_{en}$ .

**5.5** A paramagnetic sample shows a net magnetisation of  $8 \text{ Am}^{-1}$  when placed in an external magnetic field of  $0.6 \text{ T}$  at a temperature of  $4 \text{ K}$ . When the same sample is placed in an external magnetic field of  $0.2 \text{ T}$  at a temperature of  $16 \text{ K}$ , the magnetisation will be

- (a)  $\frac{32}{3} \text{ Am}^{-1}$
- (b)  $\frac{2}{3} \text{ Am}^{-1}$
- (c)  $6 \text{ Am}^{-1}$
- (d)  $2.4 \text{ Am}^{-1}$ .

## MCQ II

**5.6**  $S$  is the surface of a lump of magnetic material.

- (a) Lines of  $\mathbf{B}$  are necessarily continuous across  $S$ .
- (b) Some lines of  $\mathbf{B}$  must be discontinuous across  $S$ .
- (c) Lines of  $\mathbf{H}$  are necessarily continuous across  $S$ .
- (d) Lines of  $\mathbf{H}$  cannot all be continuous across  $S$ .

- 5.7** The primary origin(s) of magnetism lies in
- atomic currents.
  - Pauli exclusion principle.
  - polar nature of molecules.
  - intrinsic spin of electron.
- 5.8** A long solenoid has 1000 turns per metre and carries a current of 1 A. It has a soft iron core of  $\mu_r = 1000$ . The core is heated beyond the Curie temperature,  $T_c$ .
- The **H** field in the solenoid is (nearly) unchanged but the **B** field decreases drastically.
  - The **H** and **B** fields in the solenoid are nearly unchanged.
  - The magnetisation in the core reverses direction.
  - The magnetisation in the core diminishes by a factor of about  $10^8$ .
- 5.9** Essential difference between electrostatic shielding by a conducting shell and magnetostatic shielding is due to
- electrostatic field lines can end on charges and conductors have free charges.
  - lines of **B** can also end but conductors cannot end them.
  - lines of **B** cannot end on any material and perfect shielding is not possible.
  - shells of high permeability materials can be used to divert lines of **B** from the interior region.
- 5.10** Let the magnetic field on earth be modelled by that of a point magnetic dipole at the centre of earth. The angle of dip at a point on the geographical equator
- is always zero.
  - can be zero at specific points.
  - can be positive or negative.
  - is bounded.

### VSA

- 5.11** A proton has spin and magnetic moment just like an electron. Why then its effect is neglected in magnetism of materials?
- 5.12** A permanent magnet in the shape of a thin cylinder of length 10 cm has  $M = 10^6$  A/m. Calculate the magnetisation current  $I_M$ .
- 5.13** Explain quantitatively the order of magnitude difference between the diamagnetic susceptibility of  $N_2$  ( $\sim 5 \times 10^{-9}$ ) (at STP) and Cu ( $\sim 10^{-5}$ ).

- 5.14** From molecular view point, discuss the temperature dependence of susceptibility for diamagnetism, paramagnetism and ferromagnetism.
- 5.15** A ball of superconducting material is dipped in liquid nitrogen and placed near a bar magnet. (i) In which direction will it move? (ii) What will be the direction of its magnetic moment?

### SA

- 5.16** Verify the Gauss's law for magnetic field of a point dipole of dipole moment  $\mathbf{m}$  at the origin for the surface which is a sphere of radius  $R$ .
- 5.17** Three identical bar magnets are rivetted together at centre in the same plane as shown in Fig. 5.1. This system is placed at rest in a slowly varying magnetic field. It is found that the system of magnets does not show any motion. The north-south poles of one magnet is shown in the Fig. 5.1. Determine the poles of the remaining two.

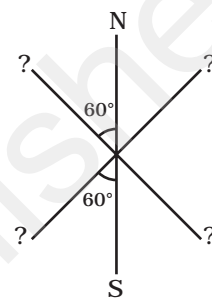


Fig. 5.1

- 5.18** Suppose we want to verify the analogy between electrostatic and magnetostatic by an explicit experiment. Consider the motion of (i) electric dipole  $\mathbf{p}$  in an electrostatic field  $\mathbf{E}$  and (ii) magnetic dipole  $\mathbf{m}$  in a magnetic field  $\mathbf{B}$ . Write down a set of conditions on  $\mathbf{E}$ ,  $\mathbf{B}$ ,  $\mathbf{p}$ ,  $\mathbf{m}$  so that the two motions are verified to be identical. (Assume identical initial conditions.)
- 5.19** A bar magnet of magnetic moment  $m$  and moment of inertia  $I$  (about centre, perpendicular to length) is cut into two equal pieces, perpendicular to length. Let  $T$  be the period of oscillations of the original magnet about an axis through the mid point, perpendicular to length, in a magnetic field  $\mathbf{B}$ . What would be the similar period  $T'$  for each piece?
- 5.20** Use (i) the Ampere's law for  $\mathbf{H}$  and (ii) continuity of lines of  $\mathbf{B}$ , to conclude that inside a bar magnet, (a) lines of  $\mathbf{H}$  run from the  $N$  pole to  $S$  pole, while (b) lines of  $\mathbf{B}$  must run from the  $S$  pole to  $N$  pole.

### LA

- 5.21** Verify the Ampere's law for magnetic field of a point dipole of dipole moment  $\mathbf{m} = m\hat{\mathbf{k}}$ . Take  $C$  as the closed curve running clockwise along (i) the  $z$ -axis from  $z = a > 0$  to  $z = R$ ; (ii) along the quarter circle of radius  $R$  and centre at the origin, in the first quadrant of  $x$ - $z$  plane; (iii) along the  $x$ -axis from  $x = R$  to  $x = a$ , and (iv) along the quarter circle of radius  $a$  and centre at the origin in the first quadrant of  $x$ - $z$  plane.

**5.22** What are the dimensions of  $\chi$ , the magnetic susceptibility? Consider an H-atom. Guess an expression for  $\chi$ , upto a constant by constructing a quantity of dimensions of  $\chi$ , out of parameters of the atom:  $e$ ,  $m$ ,  $v$ ,  $R$  and  $\mu_0$ . Here,  $m$  is the electronic mass,  $v$  is electronic velocity,  $R$  is Bohr radius. Estimate the number so obtained and compare with the value of  $|\chi| \sim 10^{-5}$  for many solid materials.

**5.23** Assume the dipole model for earth's magnetic field  $B$  which is given

$$\text{by } B_v = \text{vertical component of magnetic field} = \frac{\mu_0}{4\pi} \frac{2m \cos \theta}{r^3}$$

$$B_H = \text{Horizontal component of magnetic field} = \frac{\mu_0}{4\pi} \frac{\sin \theta m}{r^3}$$

$\theta = 90^\circ - \text{lattitude as measured from magnetic equator.}$

Find loci of points for which (i)  $|\mathbf{B}|$  is minimum; (ii) dip angle is zero; and (iii) dip angle is  $\pm 45^\circ$ .

**5.24** Consider the plane  $S$  formed by the dipole axis and the axis of earth. Let  $P$  be point on the magnetic equator and in  $S$ . Let  $Q$  be the point of intersection of the geographical and magnetic equators. Obtain the declination and dip angles at  $P$  and  $Q$ .

**5.25** There are two current carrying planar coils made each from identical wires of length  $L$ .  $C_1$  is circular (radius  $R$ ) and  $C_2$  is square (side  $a$ ). They are so constructed that they have same frequency of oscillation when they are placed in the same uniform  $\mathbf{B}$  and carry the same current. Find  $a$  in terms of  $R$ .